

STUDY GUIDE

INCREASING / DECREASING INTERVALS: Use 1st Derivative

- 1.) Find $f'(x)$
- 2.) Find critical numbers for $f'(x)$
- 3.) Place the critical numbers on a number line and pick test values on each interval
- 4.) Replace these test values in $f'(x)$ to determine " + " or " - "
 - " + " → Increasing
 - " - " → Decreasing
- 5.) Write your results using interval notation

LOCAL MAXIMUM / LOCAL MINIMUM:

- Use First Derivative Test
- These are found when a function changes from [no VA]:
 - Increasing to decreasing Local Maximum
 - Decreasing to increasing Local Minimum
- Be sure to write in point form!!!

INTERVALS OF CONCAVITY: Use 2nd Derivative

- 1.) Find $f''(x)$
- 2.) Find critical points for $f''(x)$
- 3.) Place critical points on a number line and pick test values on each interval
- 4.) Replace these test values in $f''(x)$ to determine " + " or " - "
 - " + " → Concave UP
 - " - " → Concave DOWN
- 5.) Write your results using interval notation

POINTS OF INFLECTION:

- These are found when a continuous function changes from [no VA]:
 - Concave up to concave down
 - Concave down to concave up
- Be sure to write in point form!!!

REVIEW

- 1.) Find the intervals where the function is increasing and decreasing. Then use the First Derivative Test to identify the local maximum and local minimum value(s).

$$f(x) = x^3 - 75x$$

- 2.) Find the intervals of concavity for the function. Then identify all points of inflection.

$$f(x) = x^4 - 4x^3 + 10x - 9$$

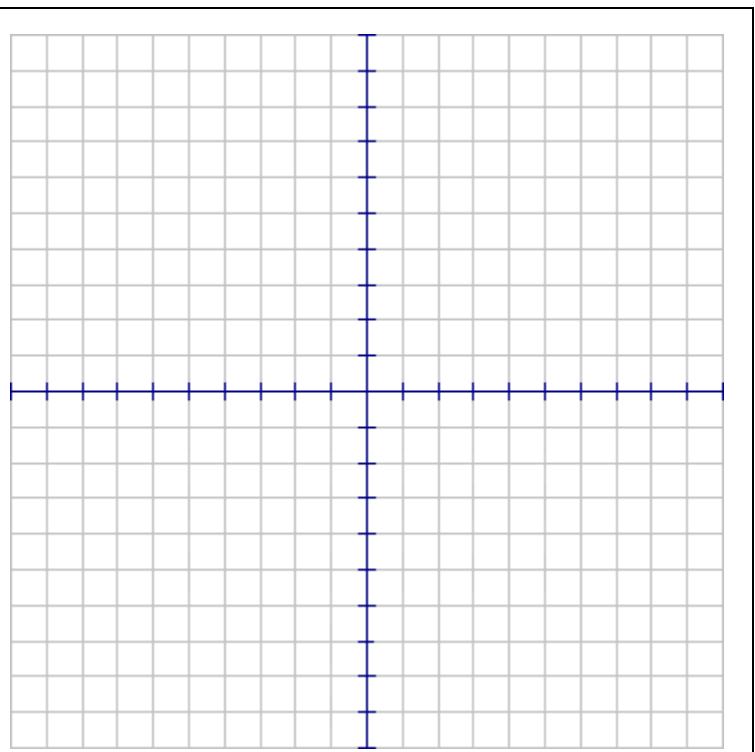
Directions: Given the function, find all information then sketch a graph.

3.) $f(x) = x^3 - 3x^2 + 4$

$f'(x) = \underline{\hspace{10cm}}$

$f''(x) = \underline{\hspace{10cm}}$

DOMAIN	
x -intercept(s)	y -intercept
HOLE(S)	VA's
HA's	SA's
INCREASING	DECREASING
LOCAL MAXIMUM(S)	LOCAL MINIMUM(S)
CONCAVE UP	CONCAVE DOWN
POINT(S) OF INFLECTION	



SHOW ALL WORK HERE

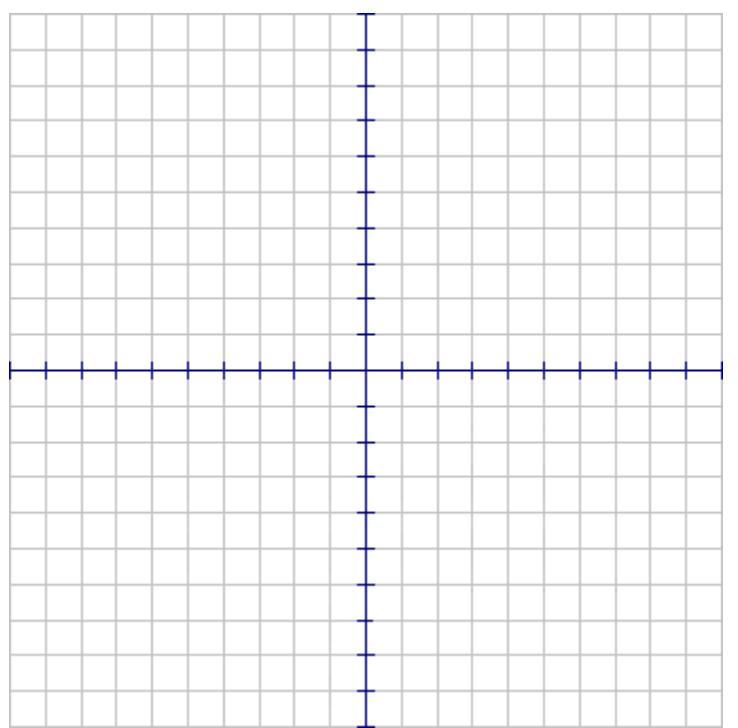
Directions: Given the function, find all information then sketch a graph.

4.) $f(x) = \frac{x^2+1}{x}$

$$f'(x) = \underline{\hspace{10cm}}$$

$$f''(x) = \underline{\hspace{10cm}}$$

DOMAIN	
x -intercept(s)	y -intercept
HOLE(S)	VA's
HA's	SA's
INCREASING	DECREASING
LOCAL MAXIMUM(S)	LOCAL MINIMUM(S)
CONCAVE UP	CONCAVE DOWN
POINT(S) OF INFLECTION	



SHOW ALL WORK HERE

Directions: Determine if the statement is TRUE or FALSE.

- _____ 5.) All polynomials are continuous.
- _____ 6.) A critical point is a location where change will occur.
- _____ 7.) A point of inflection will result in a change in concavity.
- _____ 8.) Concavity represents how the slope of a function is changing.
- _____ 9.) A change in concavity must occur at a point of inflection.
- _____ 10.) The local minimum is the minimum height of the function.
- _____ 11.) The local maximum represents a change in the slope of a function from increasing to decreasing.
- _____ 12.) Local extrema are the result of a change in slope on a graph.
- _____ 13.) Critical points on the second derivative are potential points of inflection.
- _____ 14.) Critical points on the first derivative of a polynomial represent where a horizontal tangent exists.
- _____ 15.) The maximum height on a graph can be the local maximum.
- _____ 16.) A vertical asymptote will always result in a critical point.
- _____ 17.) When the first derivative equals zero, it results in local extrema.
- _____ 18.) Relative minimum is another name for the local minimum.

SOLUTIONS

1.) Increasing: $(-\infty, -5) \cup (5, \infty)$

Decreasing: $(-5, 5)$

Local Max: $(-5, 250)$

Local Min: $(5, -250)$

3.) $f(x) = x^3 - 3x^2 + 4$

$f'(x) = 3x^2 - 6x$

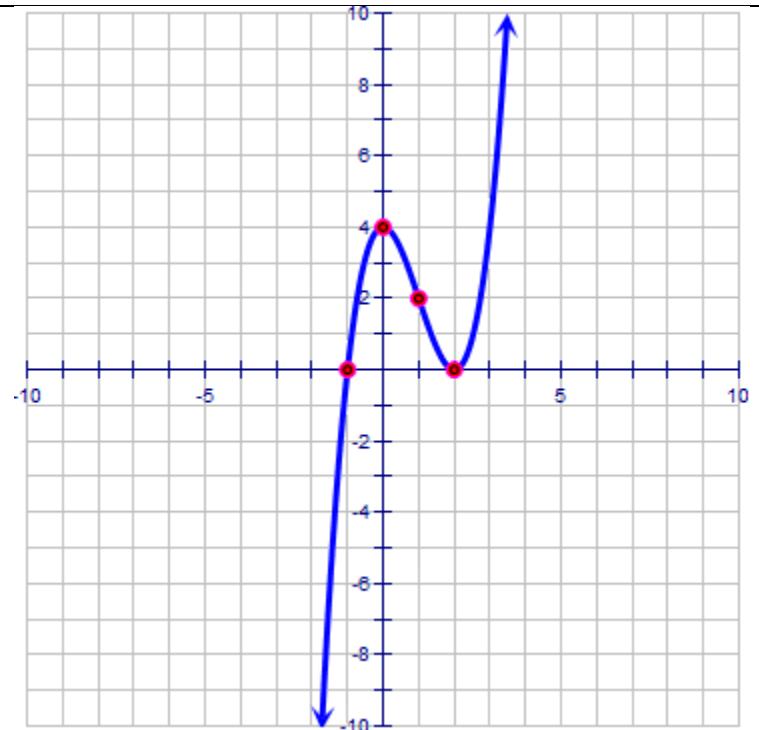
2.) Concave UP: $(-\infty, 0) \cup (2, \infty)$

Concave DOWN: $(0, 2)$

Pts of Inflection: $(0, -9)$ and $(2, -5)$

$f''(x) = 6x - 6$

DOMAIN	
$(-\infty, \infty)$	
x -intercept(s)	y -intercept
$(-1, 0)$ and $(2, 0)$	$(0, 4)$
HOLE(S)	VA's
none	none
HA's	SA's
none	none
INCREASING	DECREASING
$(-\infty, 0) \cup (2, \infty)$	$(0, 2)$
LOCAL MAXIMUM(S)	LOCAL MINIMUM(S)
$(0, 4)$	$(2, 0)$
CONCAVE UP	CONCAVE DOWN
$(1, \infty)$	$(-\infty, 1)$
POINT(S) OF INFLECTION	
$(1, 2)$	

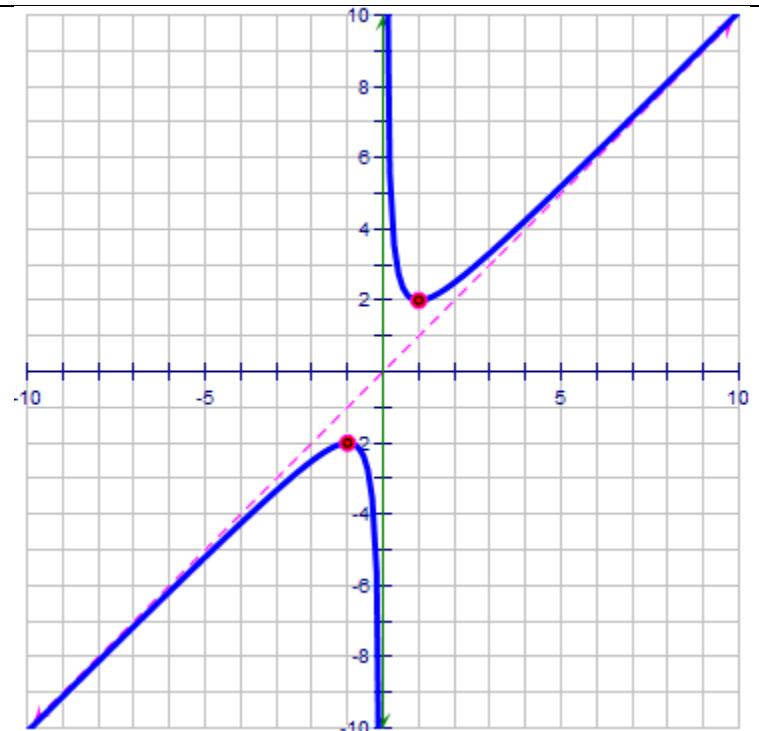


4.) $f(x) = \frac{x^2+1}{x}$

$f'(x) = \frac{x^2-1}{x}$

$f''(x) = \frac{2}{x^3}$

DOMAIN	
$(-\infty, 0) \cup (0, \infty)$	
x -intercept(s)	y -intercept
none	none
HOLE(S)	VA's
none	$x = 0$
HA's	SA's
none	$y = x$
INCREASING	DECREASING
$(-\infty, -1) \cup (1, \infty)$	$(-1, 0) \cup (0, 1)$
LOCAL MAXIMUM(S)	LOCAL MINIMUM(S)
$(-1, -2)$	$(1, 2)$
CONCAVE UP	CONCAVE DOWN
$(0, \infty)$	$(-\infty, 0)$
POINT(S) OF INFLECTION	
none	



5.) TRUE

6.) FALSE

7.) TRUE

8.) TRUE

9.) FALSE

10.) FALSE

11.) TRUE

12.) FALSE

13.) TRUE

14.) TRUE

15.) TRUE

16.) TRUE

17.) FALSE

18.) TRUE